## NUMBERS AND ALGEBRA

- Number sets N, Z, Q, R i C
  - understand number sets N, Z, Q, R and C (natural numbers, integers, rational numbers, real numbers and complex numbers)
  - compare numbers
  - o understand and use intervals and interval notation
  - $_{\odot}$   $\,$  write down subsets of real numbers as intervals and represent them on a number line
  - use standard and trigonometric form of complex numbers
- Elementary operations
  - o add, subtract, multiply and divide
  - o determine the rounded numbers and the absolute value of the numbers
  - use a calculator
- Percentage and ratios
  - o understand and use percentages
  - o understand and use ratios
- Algebraic expression and algebraic fractions
  - calculate with powers and roots
  - o add, subtract and multiply algebraic expressions
  - use identities for square and cub of binomial, for difference of squares and cubes and for sum of
  - o add, subtract, multiply and divide algebraic fractions
  - o isolating a one variable by another from algebraic equation
  - o understand and apply binominal theorem
- Units of measurements
  - use fundamental measures (units of length, , area, volume, mass, time and money)
  - Convert unit of measurement
  - Use unit of measurement in geometry and word problems
- Mathematical modeling
  - apply mathematical models related to algebraic expressions and calculations to solve problems in everyday life

#### **FUNCTIONS**

- Functions definition of a function
  - $_{\odot}$   $\,$  use functions define algebraically, graphically, numerically in tables, or by verbal descriptions
  - o add, subtract, multiply, divide and compose functionsž
- Linear and quadratic functions, absolute value functions, second root function, polynomial and rational functions, exponential and logarithmic functions, trigonometric functions
  - o determine the domain of a function

- o find the image of a function
- o calculate function values
- o draw/sketch/construct the graph of a function
- $\circ$  sketch the table of a function
- $\circ$  interpret the graph of a function
- $\circ$  calculate zeros of the function
- $_{\circ}$  find the point of intersection between function graph and x/y-axis
- $\circ$  determine the function which corresponds to the given graph
- o determine intervals on which the function increases/decreases
- interpret the graph of the function
- o determine if a function is even or odd
- Quadratic functions
- o determine coefficients and discriminate
- $_{\circ}$   $\,$  find the local minimum/maximum and the vertex of parabola  $\,$
- Polynomial and rational functions
- draw the graph of polynomials (of degree 1, 2 and 3)
- draw the graph of rational function (with polynomials of degree 1 or 2 in numerator and denominator)
- Exponential and logarithmic functions
- draw the graph of composition of linear and exponential or logarithmic functions
- o apply exponential and logarithmic basic identities
- Trigonometric functions
- $_{\circ}$   $\,$  define trigonometric functions on the unit circle
- determine the fundamental period of a function and apply properties of periodic function to trigonometric functions
- $_{\circ}$   $\,$  use basic trigonometric identities
- $\circ \quad$  apply trigonometric formulas for angle sum
- o apply product-to-sum and sum-to-product trigonometric identities
- recognize and graph trigonometric functions of thr form
  - f(x) = Asin(Bx C) D
  - $f(x) = A\cos(Bx C) D$
- Sequences
  - $\circ$  recognize the given sequences
  - o recognize the arithmetic sequences
  - $_{\circ}$   $\,$  determine the nth term and the term sum of arithmetic sequence
  - recognize the geometric sequences
  - $\circ$   $\,$  determine the nth term and the term sum of geometric sequence
- Derivation of functions
  - find derivation of the constant function, polynomial functions and trigonometric functions
  - $_{\odot}$   $\,$  find the derivation of the sum, difference, product, quotient and composition of functions  $\,$
  - determine the tangent line at a point of the graph of the differential function
  - use the differential calculus to analyze functions
  - apply mathematical models related to algebraic expressions and calculations to solve problems in everyday life

- Mathematical modeling
  - $_{\odot}$   $\,$  apply mathematical models related to functions to solve problems in everyday life

# EQUATIONS AND INEQUATIONS

- Linear equations and inequations
  - solve linear equations and inequations
- Quadratic equations and inequations
  - $_{\circ}$   $\,$  solve quadratic equations and inequations
  - use Vieta's formulas
- Absolute value equations and inequations, root equations and inequations
  - o solve absolute value equations and inequations
  - solve root equations and inequations
- Simple polynomials and rational equations and inequations
  - solve equations/ inequations by factoring
  - solve equations/ inequations by substitution; for instance biquadratic equation
- Exponential and logarithmic equations and inequations
  - $_{\circ}$   $\,$  solve exponential equations/ inequations with same base
  - solve equations/ inequations using definition of logarithm
  - solve equations/ inequations by logarithm both sides of equation/inequation
  - solve equations/inequations using basic properties of logarithms and exponents
  - solve equations/inequations which can be reduced to quadratic equation/inequation by substitution
- Trigonometric equations
  - find general and particular solution of trigonometric equation using definition of trigonometric functions
  - find general and particular solution of trigonometric equation using trigonometric identities
- Systems of equations and inequations
  - o solve systems of equations or inequations algebraically and graphically
  - explain graphical solutions of system of equations or inequations
- Mathematical modeling
  - use mathematical models related to equations or inequations to solve problems in everyday life

### **BASIC GEOMETRY**

- Geometry basics in planimetry
  - $_{\circ}$  measure angles
  - $\circ$  classify triangles
  - $_{\circ}$   $\,$  use notions of congruent and similar triangles  $\,$

- o determine congruent triangles
- o determine similar triangles
- calculate the scale (homotetic) factor
- apply Pythagorean theorem
- o use properties of parallelograms, trapezoids and regular polygons
- determine and use parts of circle and disc (center, radius, arc, sector, central and inscribed angle, chord and tangent)
- use the Inscribed angle theorem and Thales theorem
- $_{\circ}$   $\,$  calculate the area and the circumference of circle
- Interrelation among geometric objects in tree-dimensional space
  - o determine the relationship between lines and planes in 3D space
  - $_{\circ}$  determine the intersection of a line and plane in 3D space
  - determine the orthogonal projection of a point and a line segment onto a plane
  - determine the angle between two lines and between a line and a plane
- Geometry basics in stereometry (prisms, pyramids, cylinders, cones, sphere)
  - recognize and name of these solids
  - determine parts of these solids (base, apex, height altitude, lateral faces)
  - o find the surface area and the volume of these solids

### TRIGONOMETRY

- Trigonometry for right-angle triangles; Trigonometry for scalene triangles
  - use the definition of sine, cosine and tangent in a right-angled triangle
  - use the law of sine and the low of cosine
  - o aplly trigonometry in planimetry and stereometry (solid geometry)

### ANALYTIC GEOMETRY

- Coordinate system on a line and on a plane
  - read and plot coordinates in the coordinate system
  - o calculate the distance between two given points
  - find the coordinates of the midpoint of a line segment
- Vectors

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- $\circ$  understand vector operations
- o use coordinate vector
- find the length of a vector
- find the angle between two vectors
- Equations of a line
  - use explicit and implicit equation of a line
  - o find the equation of the line given by a point and a slope
  - o find the equation of the line given by two points
  - find the angle between two lines
  - o use the condition for parallel and perpendicular lines

- o calculate the distance from a point to a line
- Second-order curves
  - $_{\circ}$   $\,$  determine the equation of a circle in standard form
  - o determine the equation of a ellipse in standard form
  - determine the equation of a hyperbola in standard form and find the equation of asymptotes
  - determine the equation of a parabola in standard form
  - find the interrelation between a second-order curve and a line
  - determine the equation of tangent line to a curve
  - apply the condition for a line to be tangent to the second –order curve
- Mathematical modeling
  - use mathematical models related to geometry to solve problems in everyday life